SEMESTER-II

COURSE 1: DIFFERENTIAL EQUATIONS

5 hrs/week Theory Credits: 4

Course Outcomes

After successful completion of this course, the student will be able to

- 1. solve first order first degree linear differential equations.
- 2. convert a non-exact homogeneous equation to exact differential equation by using an integrating factor.
- 3. know the methods of finding solution of a differential equation of first order but not of first
- 4. solve higher-order linear differential equations for both homogeneous and non-homogeneous, with constant coefficients.
- 5. understand and apply the appropriate methods for solving higher order differential equations.

Course Content

Unit - 1

Differential Equations of first order and first degree

Linear Differential Equations – Bernoulli's Equations - Exact Differential Equations – Integrating factors - Equations reducible to Exact Equations by Integrating Factors -

ii)
$$\frac{1}{Mx + Ny}$$

ii)
$$\frac{1}{Mx + Ny}$$
 iii) $\frac{1}{Mx - Ny}$

Unit - 2

Differential Equations of first order but not of first degree

Equations solvable for p, Equations solvable for y, Equations solvable for x – Clairaut's equation -Orthogonal Trajectories: Cartesian and Polar forms.

Unit - 3

Higher order linear differential equations

Solutions of homogeneous linear differential equations of order n with constant coefficients -Solutions of non-homogeneous linear differential equations with constant coefficients by means of polynomial operators

(i)
$$Q(x) = e^{ax}$$
 (ii) $Q(x) = Sin ax$ (or) $Cos ax$

Unit - 4

Higher order linear differential equations (continued.)

Solution to a non-homogeneous linear differential equation with constant coefficients

P.I. of
$$f(D)y = Q$$
 when $Q = bx^k$

P.I. of
$$f(D)y = Q$$
 when $Q = e^{ax}V$, where V is a function of x

P.I. of
$$f(D)y = Q$$
 when $Q = xV$, where V is a function of x

Unit - 5

Higher order linear differential equations with non-constant coefficients

Linear differential Equations with non-constant coefficients; Cauchy-Euler Equation; Legendre Equation; Method of variation of parameters

Activities

Seminar/ Quiz/ Assignments/ Applications of Differential Equations to Real life Problem / Problem Solving Sessions.

Text Book

Differential Equations and Their Applications by Zafar Ahsan, published by Prentice-Hall of India Pvt. Ltd, New Delhi-Second edition.

Reference Books

- 1. Ordinary and Partial Differential Equations by Dr. M.D. Raisinghania, published by S. Chand & Company, New Delhi.
- 2. Differential Equations with applications and programs S. Balachandra Rao & HR Anuradha-Universities Press.
- 3. Differential Equations -Srinivas Vangala&Madhu Rajesh, published by Spectrum University Press.
